



# Medical diagnostic systems

(Orvosbiológiai képalkotó rendszerek)

# Beamforming in ultrasound

( Nyalábalkotás az ultrahangban)

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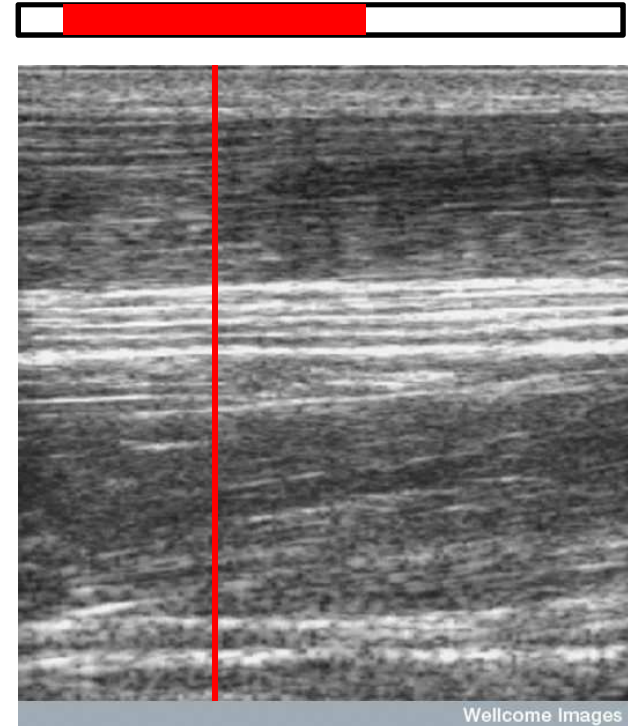
## Overview of this lecture

- Array-dependent scanning methods (linear, phased, 2-D,...)
- Beamforming strategies (fixed & dynamic focus, advanced)
- Speckle reduction techniques (compounding)
- Sidelobes and sidelobe reduction techniques (apodization)

## Linear array

- Typically higher frequencies
  - example: 5-10 MHz
  - high resolution ( $\sim 0.2$  mm)
  - short penetration depth ( $\sim 10$  cm)
- Subset of elements (subaperture) used to form each A-line
- Good for imaging organs with easy access (e.g. abdominal organs)
- Elevational (in-plane) focusing achieved using acoustic lens
  - typical resolution 10 mm
- Spacing between elements on the order of a wavelength (see “grating lobes” slides later on)

typically half (64/128 elements) of the entire aperture used to generate A-line



“Nerve movement in forearm during wrist extension”  
<http://images.wellcome.ac.uk/B0004357>  
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## Phased array

- Typically lower frequency
  - example: 1-4 MHz
  - low resolution (~0.6 mm)
  - large penetration depth (~30 cm)
- Good for imaging deep, hard-to-access (limited acoustic window e.g. due to ribs) organs (e.g. heart)
- Elevational (in-plane) focusing achieved using acoustic lens
  - typical resolution 14 mm ?
- Spacing between elements less than half a wavelength (see “grating lobes” slides later on)

entire aperture active in generating A-line



“Ultrasound image of normal 24 week fetus”  
<http://images.wellcome.ac.uk> N0019385  
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## Arrays for 3-D imaging

Freehand 1D array (position feedback with e.g. optical markers)

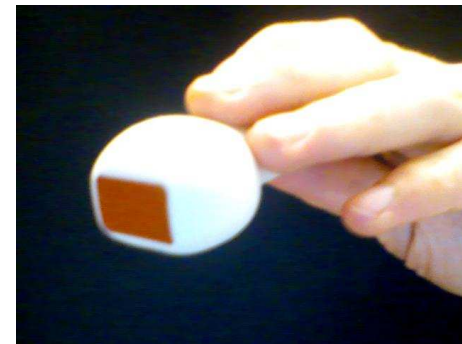
- difficult registration (may be aided by position sensing)
- + simple to use

Mechanised 1D array (fixed, predictable motion e.g. inside casing)

- inflexible
- + simple registration

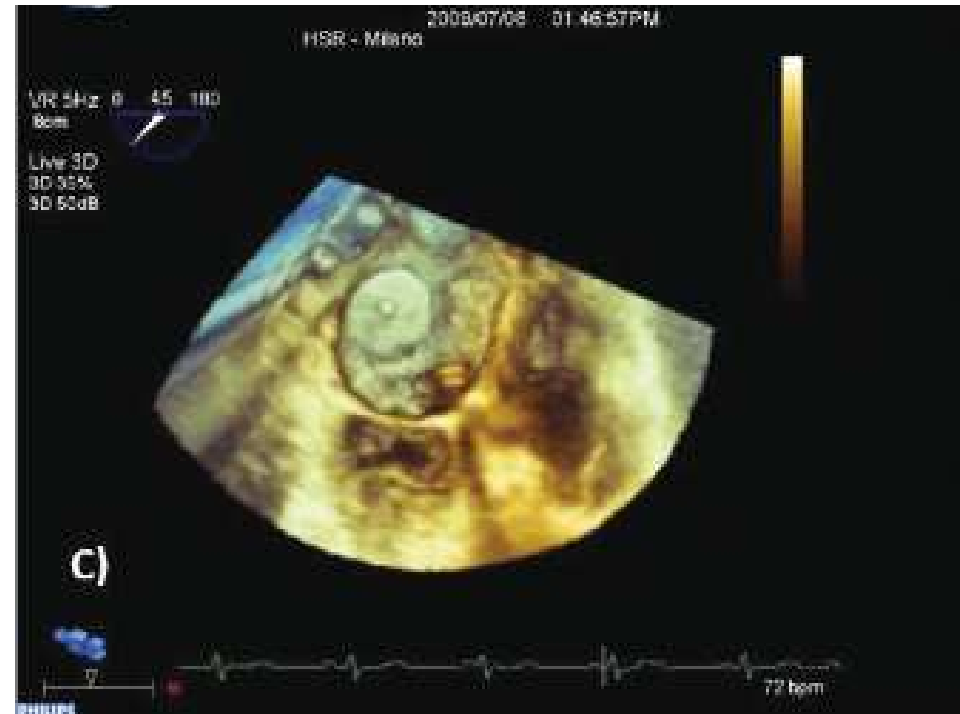
2D array

- electronic complexity
- element spacing
- + real-time 3D



x7-2 array from Philips with 50x50 elements

## 3-D visualisation: surface vs. volume rendering



Courtesy of Zonare Medical Systems  
[http://www.zonare.com/products/clinical-images/id\\_7/](http://www.zonare.com/products/clinical-images/id_7/)

3D US image of left atrium [Agricola *et al.* 2010]  
Creative Commons Attribution 3.0 Licence  
<http://www.pagepress.org/journals/index.php/hi/article/viewArticle/hi.2010.e6/2133>

## Other types of array

- Annular (concentric rings) [Anderson 2006]
  - accurate focusing along axis to produce A-line
  - need to be moved to provide B-mode
- Element(s) inside catheter [Cobbold pp. 580-593]
  - single element moving inside catheter *OR* ring of elements used as phase array
  - exciting applications for imaging inside vessels, e.g. intravascular ultrasound (IVUS)



“Normal prostate”

<http://images.wellcome.ac.uk/>

N0013084

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**For now, concentrate discussion of beamforming on 1-D arrays (linear and phased)**



### Beamforming strategies

- Fixed delay (near-field, far-field)
- Dynamic focusing: vary receive beam with focus
- Focal zone splicing: several transmission depths
- Parallel receive beamforming (access to pre-beamformed data)
- Synthetic aperture imaging (access to pre-beamformed data)



## Fixed delay beamforming

Example: two transceivers A, B; point scatterer S

- Estimation of scatterer strength becomes minimum-variance (electrical noise, “spatial noise” from other scatterers) combination of two transmissions and two receptions (*cf.* beamforming as spatial filtering [Van Veen and Buckley 1988])

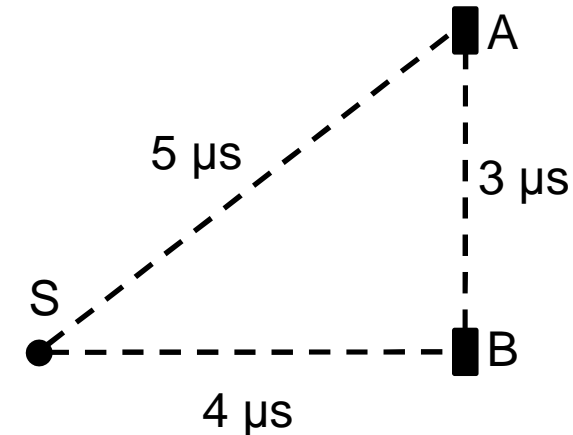
- Transmit: delay B by  $1 \mu\text{s}$

$$y_A(t) = w(t); \quad y_B(t) = w(t-1)$$

- Signals received in phase at  $5 \mu\text{s}$
- Receive: delay A by  $1 \mu\text{s}$  (relative to B); sum

$$b(t) = y_A(t-5) + y_B(t-4)$$

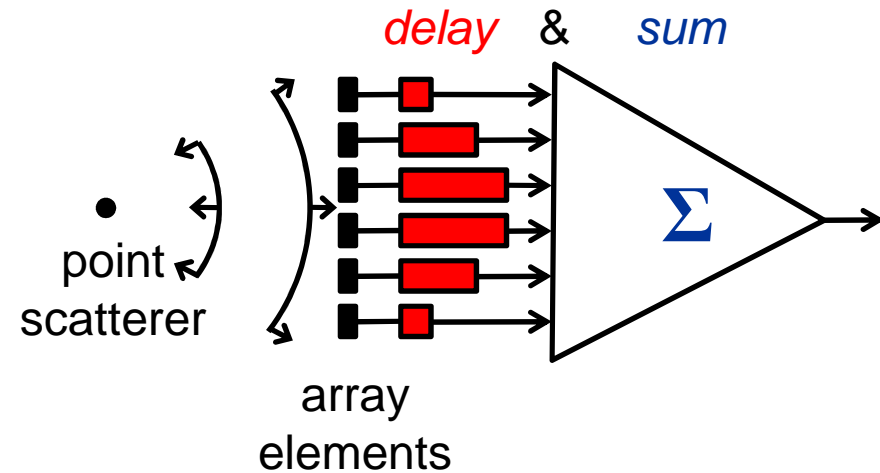
- *Delay-and-sum beamforming* on receive



## Fixed delay beamforming

- Simplest beamforming method
- Same focus for transmit and receive
- $\Delta\text{transmit\_delays} = -\Delta\text{receive\_delays}$
- Sharp focusing at target depth, but blurring at other depths
- Far-field limit  $\rightarrow$  plane wave
- plane wave  $\rightarrow$  linear variation of delays

Example:  $D=10$  mm,  $c=1500$  m/s,  $f=1.5$  MHz. Far-field from  $D^2/4\lambda = 25$  mm

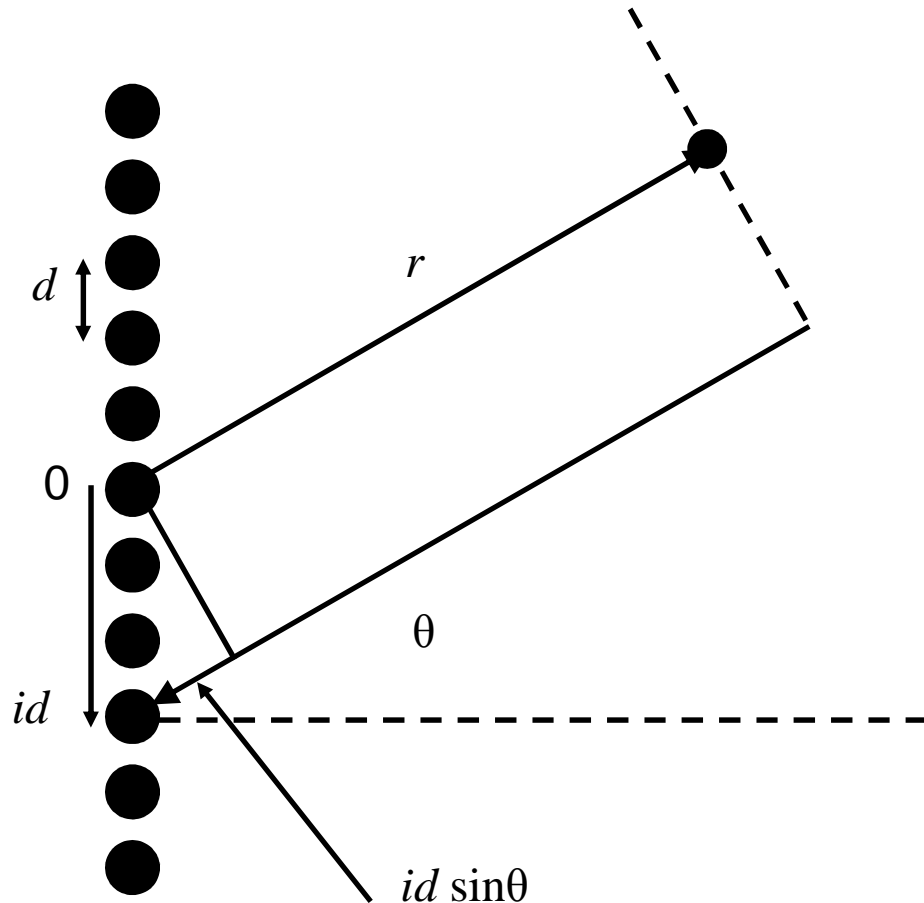


Fixed delay-and-sum beamforming on Tx, Rx.  
Adapted from [Burns 2005]

## Phased array beamforming (far-field)

- Reference time ( $t=0$ ) when pulse is transmitted from central element
- Usually, number of elements is even...
- Fix relative delays, then scale time to distance accordingly
- Delay given by

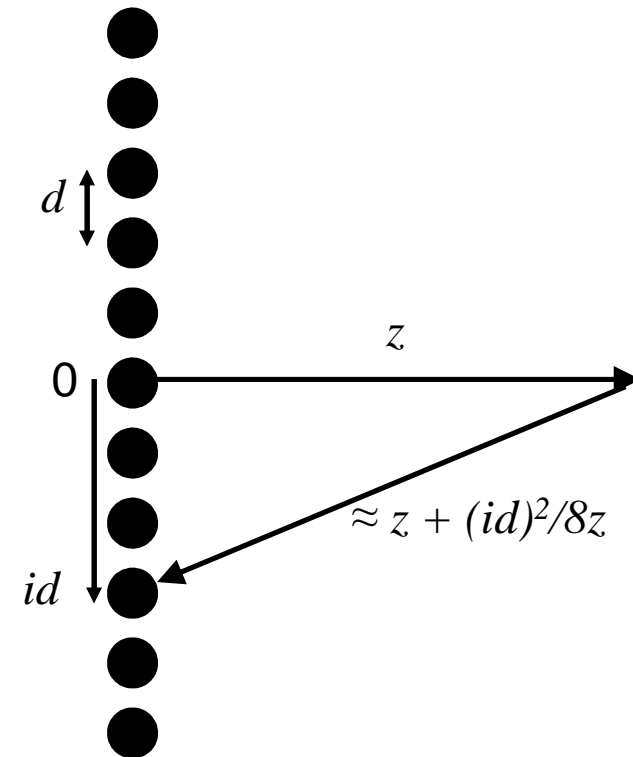
$$\tau(i,r) = 2r/c + id \sin\theta$$



## Dynamic receive beamforming

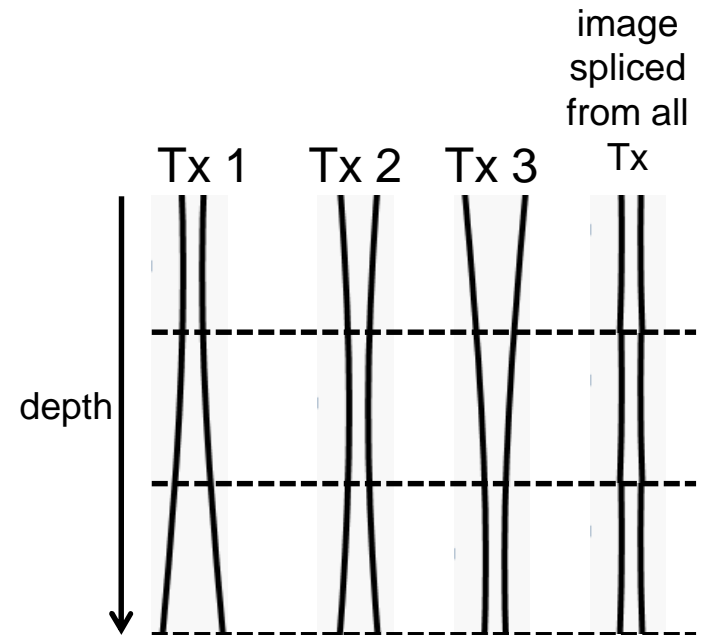
- Once electric pulse converted into acoustic pulse (transmission), no user control over pulse propagation (single beam is formed)
- Beamforming on receive, however, occurs electronically/digitally and any number of beams can be synthesised
- Observation: as echoes return, they come from deeper and deeper objects
- Idea: dynamically vary receive focus with time
- Corresponds to “stretching” (frequency modulation) of signal for out-of-centre elements
- Delay given by

$$\tau(i, r) = 2z/c + (id)^2/8z$$



## Focal zone splicing

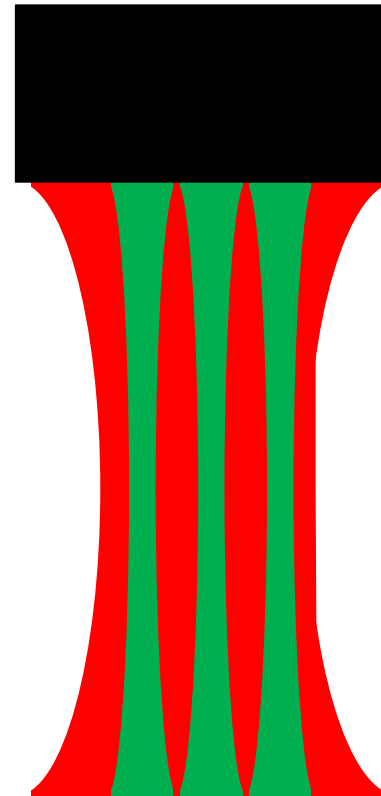
- Well-focussed transmit beam leads to good *local* sharpness
- Transmit several pulses with different foci
- Splice resulting images together
- Reduction in frame rate
- See [Szabo2004, p.309] for images



adapted from [B-K Medical 2003, p. 59]

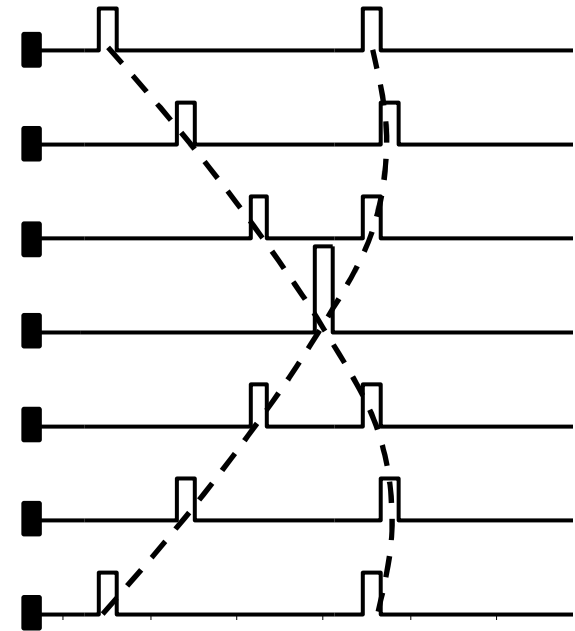
## Parallel receive beamforming: zone focussing

- Frame rate depends on number of transmissions
- With parallel digitization of element signals, several **receive beams** can be synthesised for a single, broader, **transmit beam**
- Zonare Medical Systems ([www.zonare.com](http://www.zonare.com)) uses this technology



### Parallel receive beamforming: multiple beam transmission

- Several transmit beams synthesised in one transmission
- Parallel acquisition allows receive focussing (and thus separation) of the beams
- Again, increase in frame rate results



simultaneous synthesis of two beams  
adapted from [Cobbold 2007, p.476]

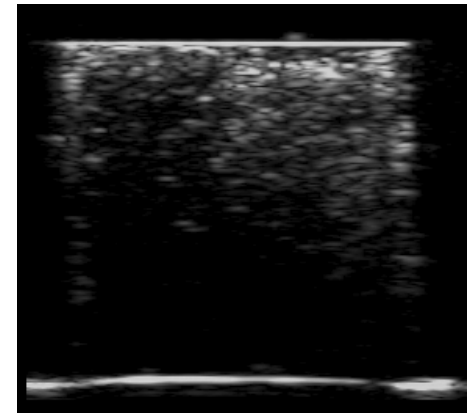
### Synthetic aperture imaging *[Jensen et al. 2007]*

- Each element transmits a pulse on its own, one after the other
- Echoes recorded by all (or many elements) at once
- Assuming linearity, principle of superposition applies
- Both transmit and receive foci can be synthesised retrospectively!
- Higher image resolution
- See *[Jensen et al. 2007]* for images



### Speckle reduction techniques

- Speckle arises from interference between sub-wavelength scatterers from within one resolution cell
- Spatial averaging (blurring) reduces speckle, but also reduces spatial resolution
- Compounding
  - generate several images with different parameters
  - speckle hopefully weakly correlated
  - sum images to reduce speckle “noise”
  - averaging frames (temporal) causes blurring
  - look at two popular methods: spatial; frequency



Speckle in B-mode image of agar gel. Notice that speckle has rice-like shape, elongated about the transverse direction.

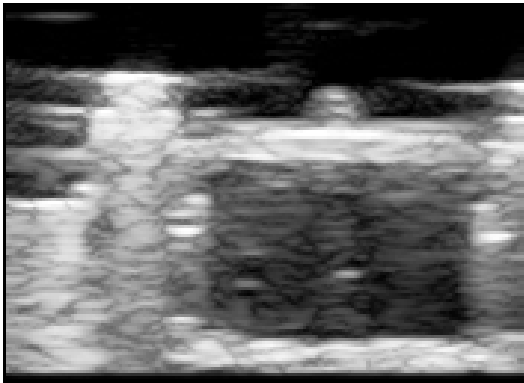
### Spatial/angular compounding [Cobbold 2007, p. 469]

- Subject imaged from several orientations
- Scatterers interfere with different phases when angle of insonation/reception is varied → speckle weakly correlated
- Summation of registered images from several orientations reduces speckle
- Orientations generated from consecutive transmissions:
  - array need not move
  - frames separated by less than 100 ms
  - simple registration
  - real-time compound images

# Frequency compounding

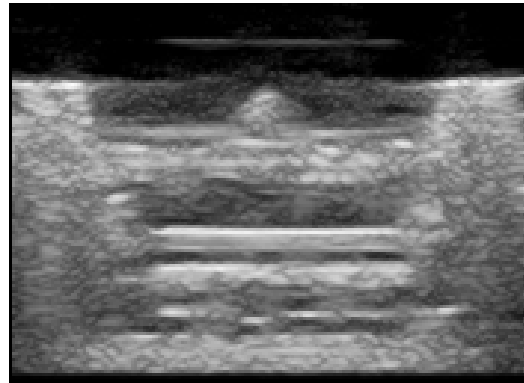
- Scattering directivity changes with frequency, but not origins of scattering
- Therefore, strong correlation between images
- Modest speckle reduction

6 MHz

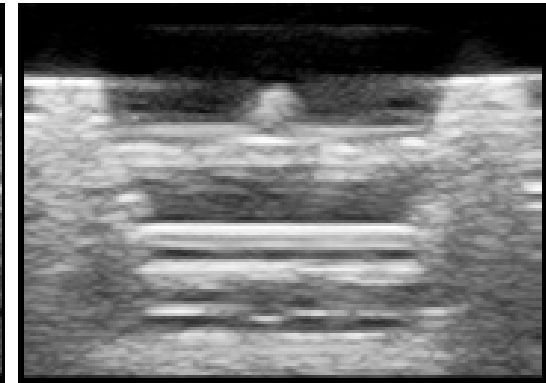


**Slightly different picture from other two. However, note increased speckle size**

8.5 MHz



compound ("C8")



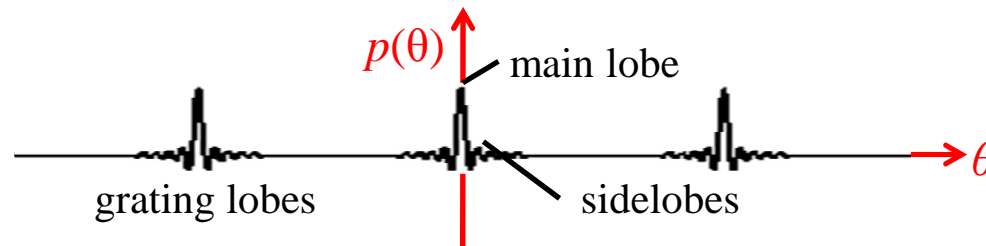
Images of tissue-mimicking agar gel with vessel-mimicking inclusion; acquired on a z.one ultrasound system (Zonare)

## Sidelobes and sidelobe reduction techniques

Sidelobes arise due to

- limited aperture
- sampled aperture (grating lobes)
- temporal quantization errors (quantization error grating lobes)

Sidelobe reduction techniques



Pressure field against angle created by transducer.  
(Note that purely angular dependence implies far-field)

### Grating lobes [Szabo 2004, pp. 182-185]

- Next lecture: in continuous wave mode, pressure in focal plane is 2-D Fourier transform of pressure amplitude distribution over aperture (i.e. apodization)
- More precisely, angular distribution of pressure is 2-D Fourier transform of apodization in far-field, and focusing brings the far-field to the focal plane
- Thus (in analogy with the Fourier sampling theorem), if the discrete element spacing “samples” at  $d \geq 0.5\lambda$ , grating lobes (“aliasing”) appear
- Grating lobes first appear at  $\theta = \pm\pi$  ( $d = 0.5\lambda$ ) and move closer to region of interest as  $d$  is further increased (new grating lobes appear every time  $d$  increased by  $0.5\lambda$ )
- Are grating lobes avoided in practice?

### Grating lobes [Szabo 2004, pp. 182-185]

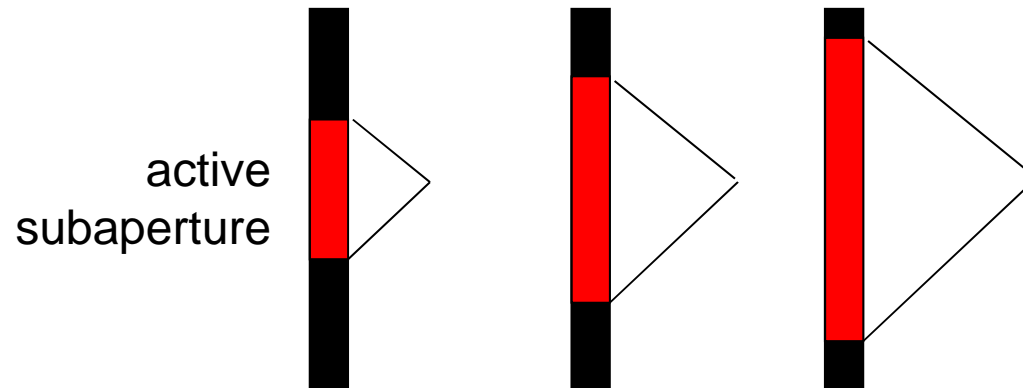
- Are grating lobes avoided in practice? Two examples:
  - L10-5 linear array:  $f_c = 7.5$  MHz,  $N=128$ ,  $D=38$  mm  $\rightarrow d = 1.5 \lambda$
  - P4-1 phased array:  $f_c = 2.5$  MHz,  $N=128$ ,  $D=28$  mm  $\rightarrow d = 0.37 \lambda$
- In linear scanning, the angle of inspection is 0, and the grating lobes are at such high angles that the interference from them is minimal (*cf.* obliquity factor reducing pressure field to 0 at  $\theta=\pi$  for soft baffles such as ultrasonic transducers [Cobbold 2007, pp. 447-448])
- Therefore, the requirement for  $d < 0.5\lambda$  is relaxed for linear arrays
- However, in phased arrays angle of inspection varies substantially (e.g.  $-\pi/4$  to  $\pi/4$ ), so grating lobes can have an effect, and  $d < 0.5\lambda$  adhered to
- Grating lobes arise naturally out of CW analysis (see next lecture). Simple way to reduce grating lobes: shorten the pulse!

### Apodization – beam shaping [Szabo 2004, p. 193]

- Again consider statement that pressure in focal plane is 2-D Fourier transform of apodization function (weightings used for the elements)
- Therefore, to provide a sharp beam (good imaging resolution) on transmit and receive, transducer should be as large as possible
- In the limiting case of an infinite plane or enveloping hemisphere, the beam would be an impulse
- However, in the case of a finite aperture, the beam smears
- This is in analogy with estimating the power spectrum of a signal from a limited time window
- As in power spectrum estimation, uniform apodization causes sinc beam
- Borrowing from spectral estimation techniques, different apodization (windowing) functions [Harris 1978] can be used to reduce the amplitude of sidelobes, *at the expense of increasing the main lobe width*

### Dynamic receive apodization

- Increase receiving subaperture with depth
- constant  $f\#$  on receive
- blurring (PSF) more uniform with depth
- easier to deconvolve blurring computationally
- easier to “deconvolve” (interpret image) by eye





## Adaptive beamforming [Holm *et al.* 2009]

- Technique taken from radar and sonar (as so often with ultrasound!)
- Original aim was to cancel out jamming signal from enemy
- Vary element weights  $\mathbf{w}$  (apodization) so as to reject signal from elsewhere
- This allows placing of sidelobes at regions of low energy (or low scattering) while maintaining position of main lobe (i.e. focus)
- Example: Capon beamformer – minimise beamformed signal energy while keeping  $|\mathbf{w}|=1$
- See [Holm *et al.* 2009] for illustrative images

## References

- [Agricola *et al.* 2010] Real-time three dimensional transesophageal echocardiography: technical aspects and clinical applications
- [Anderson 2006] A seminar on  $k$ -space applied to medical ultrasound.  
<http://dukemil.bme.duke.edu/Ultrasound/k-space/index.htm>
- [B-K Medical 2003] Users guide for casablanca engine interface
- [Burns 2005] Introduction to the physical principles of ultrasound imaging and Doppler.  
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- [Cobbold 2007] Foundations of biomedical ultrasound
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- [Szabo 2004] Diagnostic ultrasound imaging: Inside out
- [Van Veen and Buckley 1988] Beamforming: A versatile approach to spatial filtering