

# GEOGRAPHICAL ECONOMICS

## "B"

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Course Material Developed by Department of Economics,  
Faculty of Social Sciences, Eötvös Loránd University Budapest (ELTE)  
Department of Economics, Eötvös Loránd University Budapest  
Institute of Economics, Hungarian Academy of Sciences  
Balassi Kiadó, Budapest

Authors: Gábor Békés, Sarolta Rózsás

Supervised by Gábor Békés

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ELTE Faculty of Social Sciences, Department of Economics

# GEOGRAPHICAL ECONOMICS

## "B"

week 4

### Geographical economics – growth and convergence

Gábor Békés, Sarolta Rózsás

## 1 Economic Growth and International Convergence

### 1.1 The Mankiw-Romer-Weil analysis

#### Growth

Economic Growth and the neoclassical model

- Solow-Swan model
- Mankiw, G., Romer, D. and Weil, D. (1992), A contribution to the empirics of economic growth, QJE
- Once a country has a growth rate below the steady-state level, they grow at a faster rate.
- = convergence to the steady-state level, which is the same for each country.
- ... if technologies and preferences are identical.

#### MRW: basic Solow model

Solow model, Cobb-Douglas, CRS

$$Y(t) = K(t)^\alpha [A(t)L(t)]^{1-\alpha} \quad (1)$$

- $A(t)$  – total factor productivity

$$\dot{K} = sY - \delta K \quad (2)$$

- $L_t = L_0 e^{nt}$  és  $A_t = A_0 e^{gt}$
- $s$  is investment rate,  $\delta$  is depreciation rate,  $g$  is the rate of technological progress and  $n$  is the exogenous rate of population growth
- $k = K/L, y = Y/L$

$$\dot{k} = sy(t) - (n + g + \delta)k(t) = sk(t)^\alpha - (n + g + \delta)k(t) \quad (3)$$

## MRW: First results

Dependent variable: log GDP per working-age person in 1985			
Sample:	Non-oil	Intermediate	OECD
Observations:	98	75	22
CONSTANT	5.48 (1.59)	5.36 (1.55)	7.97 (2.48)
$\ln(I/GDP)$	1.42 (0.14)	1.31 (0.17)	0.50 (0.43)
$\ln(n + g + \delta)$	-1.97 (0.56)	-2.01 (0.53)	-0.76 (0.84)
$R^2$	0.59	0.59	0.01
<i>s.e.e.</i>	0.69	0.61	0.38
Restricted regression:			
CONSTANT	6.87 (0.12)	7.10 (0.15)	8.62 (0.53)
$\ln(I/GDP) - \ln(n + g + \delta)$	1.48 (0.12)	1.43 (0.14)	0.56 (0.36)
$R^2$	0.59	0.59	0.06
<i>s.e.e.</i>	0.69	0.61	0.37
Test of restriction:			
<i>p</i> -value	0.38	0.26	0.79
Implied $\alpha$	0.60 (0.02)	0.59 (0.02)	0.36 (0.15)

*Note.* Standard errors are in parentheses. The investment and population growth rates are averages for the period 1960–1985. ( $g + \delta$ ) is assumed to be 0.05.

## Results

- They confirm some important theoretical results
- The coefficients of saving and population growth have opposite signs
- We cannot reject that the two effects are equal in magnitude.
- We can explain a lot of things...
- ...but:  $\alpha$  is too high
- ...but: developed countries are different

## Augmented Solow model

TABLE II ESTIMATION OF THE AUGMENTED SOLOW MODEL			
Dependent variable: log GDP per working-age person in 1985			
Sample:	Non-oil	Intermediate	OECD
Observations:	98	75	22
CONSTANT	6.89 (1.17)	7.81 (1.19)	8.63 (2.19)
$\ln(I/GDP)$	0.69 (0.13)	0.70 (0.15)	0.28 (0.39)
$\ln(n + g + \delta)$	-1.73 (0.41)	-1.50 (0.40)	-1.07 (0.75)
$\ln(SCHOOL)$	0.66 (0.07)	0.73 (0.10)	0.76 (0.29)
$R^2$	0.78	0.77	0.24
<i>s.e.e.</i>	0.51	0.45	0.33
Restricted regression:			
CONSTANT	7.86 (0.14)	7.97 (0.15)	8.71 (0.47)
$\ln(I/GDP) - \ln(n + g + \delta)$	0.73 (0.12)	0.71 (0.14)	0.29 (0.33)
$\ln(SCHOOL) - \ln(n + g + \delta)$	0.67 (0.07)	0.74 (0.09)	0.76 (0.28)
$R^2$	0.78	0.77	0.28
<i>s.e.e.</i>	0.51	0.45	0.32
Test of restriction:			
<i>p</i> -value	0.41	0.89	0.97
Implied $\alpha$	0.31 (0.04)	0.29 (0.05)	0.14 (0.15)
Implied $\beta$	0.28 (0.03)	0.30 (0.04)	0.37 (0.12)

*Note.* Standard errors are in parentheses. The investment and population growth rates are averages for the period 1960–1985. ( $g + \delta$ ) is assumed to be 0.05. SCHOOL is the average percentage of the working-age population in secondary school for the period 1960–1985.

### MNW: Augmented model – results

- Human capital measure has a strong, significant effect
- The model explains almost 80 percent of variation in income per capita (increased)
- The sum of the coefficients is equal to zero.
- Restriction can not be rejected
- $\beta \simeq 0.3 - 0.4$
- Consistency with the data, e.g.  $Y = L^{1/3}K^{1/3}H^{1/3}$

### MNW: Conclusion

- Consistency with the data, e.g.  $Y = L^{1/3}K^{1/3}H^{1/3}$
- On the whole, these models indicate different steady state levels that are affected by exogenous determinants.
- Steady-state: accumulation of human and physical capital, growing population
- Convergence only if we control for the determinants of the steady-state
- = conditional convergence
- The speed of convergence:  $\lambda = (n + g + \delta)(1 - \alpha - \beta) \simeq 0.02$
- = GDP growth rate is the function of steady state, exogenous parameters ( $s_k, s_h, n + g + \delta$ ) and the initial level of income ( $y_0$ ) (*Deduct this result - homework!*)

## 1.2 Interpretation of convergence

### Convergence estimation

**TABLE III**  
**TESTS FOR UNCONDITIONAL CONVERGENCE**

Dependent variable: log difference GDP per working-age person 1960–1985			
	Non-oil	Intermediate	OECD
Sample:	98	75	22
Observations:			
CONSTANT	-0.266 (0.380)	0.587 (0.433)	3.69 (0.68)
ln(Y60)	0.0943 (0.0496)	-0.00423 (0.05484)	-0.341 (0.079)
$\bar{R}^2$	0.03	-0.01	0.46
s.e.e.	0.44	0.41	0.18
Implied $\lambda$	-0.00360 (0.00219)	0.00017 (0.00218)	0.0167 (0.0023)

*Note.* Standard errors are in parentheses. Y60 is GDP per working-age person in 1960.

**Convergence estimation**

**TABLE IV**  
**TESTS FOR CONDITIONAL CONVERGENCE**

Dependent variable: log difference GDP per working-age person 1960–1985			
Sample:	Non-oil	Intermediate	OECD
Observations:	98	75	22
CONSTANT	1.93 (0.83)	2.23 (0.86)	2.19 (1.17)
ln(Y60)	-0.141 (0.052)	-0.228 (0.057)	-0.351 (0.066)
ln(I/GDP)	0.647 (0.087)	0.644 (0.104)	0.392 (0.176)
ln( $n + g + \delta$ )	-0.299 (0.304)	-0.464 (0.307)	-0.753 (0.341)
$\bar{R}^2$	0.38	0.35	0.62
<i>s.e.e.</i>	0.35	0.33	0.15
Implied $\lambda$	0.00606 (0.00182)	0.0104 (0.0019)	0.0173 (0.0019)

*Note.* Standard errors are in parentheses. Y60 is GDP per working-age person in 1960. The investment and population growth rates are averages for the period 1960–1985. ( $g + \delta$ ) is assumed to be 0.05.

**Convergence estimation**

**TABLE V**  
**TESTS FOR CONDITIONAL CONVERGENCE**

Dependent variable: log difference GDP per working-age person 1960–1985			
Sample:	Non-oil	Intermediate	OECD
Observations:	98	75	22
CONSTANT	3.04 (0.83)	3.69 (0.91)	2.81 (1.19)
ln(Y60)	-0.289 (0.062)	-0.366 (0.067)	-0.398 (0.070)
ln(I/GDP)	0.524 (0.087)	0.538 (0.102)	0.335 (0.174)
ln( $n + g + \delta$ )	-0.505 (0.288)	-0.551 (0.288)	-0.844 (0.334)
ln(SCHOOL)	0.233 (0.060)	0.271 (0.081)	0.223 (0.144)
$\bar{R}^2$	0.46	0.43	0.65
<i>s.e.e.</i>	0.33	0.30	0.15
Implied $\lambda$	0.0137 (0.0019)	0.0182 (0.0020)	0.0203 (0.0020)

*Note.* Standard errors are in parentheses. Y60 is GDP per working-age person in 1960. The investment and population growth rates are averages for the period 1960–1985. ( $g + \delta$ ) is assumed to be 0.05. SCHOOL is the average percentage of the working-age population in secondary school for the period 1960–1985.

## Empirical results

- Basic setup: no convergence, poor countries do not grow faster (Table 3)
- When we take into account the steady state conditions, the effect of the initial level of income is significant and negative; conditional convergence (Table 4)
- Human capital matters, stronger convergence (Table 5)
- However, the convergence occurs as a quite slow process
- The Solow model is not so bad...

## Two concepts of convergence: remarks

- Barro and Sala-i-Martin (1995): Economic Growth, Chapter 11
- Up until now we've dealt with  $\beta$ -convergence (poor countries catching up with rich nations)
- According to another concept, convergence occurs when the dispersion of log per capita income within a group of countries declines over time. We call this process  $\sigma$ -convergence.

## Two concepts of convergence: remarks

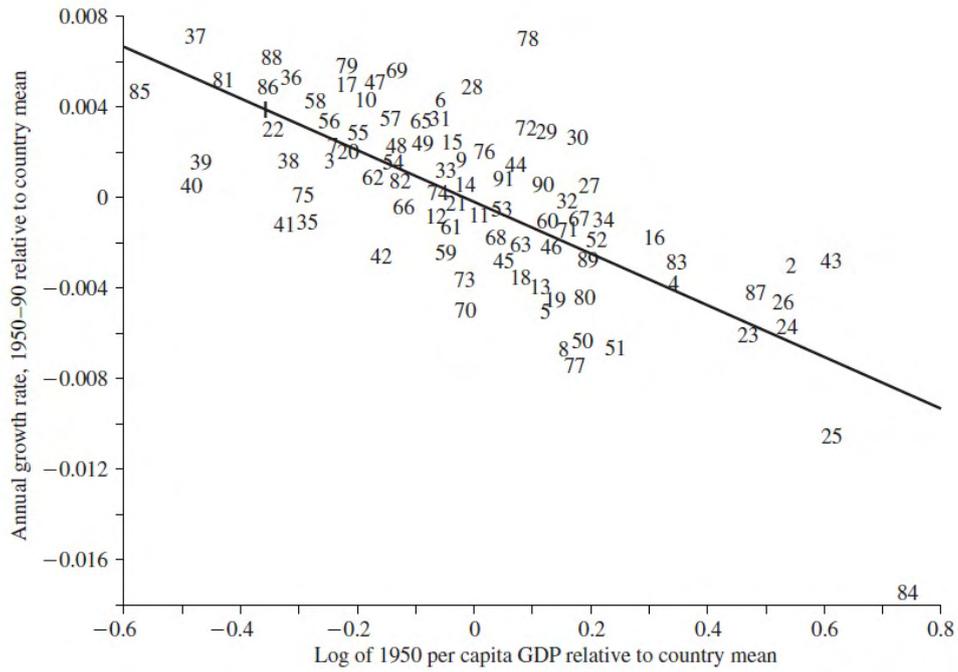
- In the case of  $\beta$ -convergence there are no overtaking or big jumps
- $\beta$ -convergence tends to generate  $\sigma$ -convergence – however, this is not a rule
- To put it in a more accurate way,  $\beta$ -convergence is a necessary but not a sufficient condition for  $\sigma$ -convergence. (*Derive this statement! - homework!*)
- The dispersion of income can be determined by exogenous shocks (e.g. oil-price shock), that affect only a limited number of countries. It can influence our convergence estimation.

## Two concepts of convergence: EU8

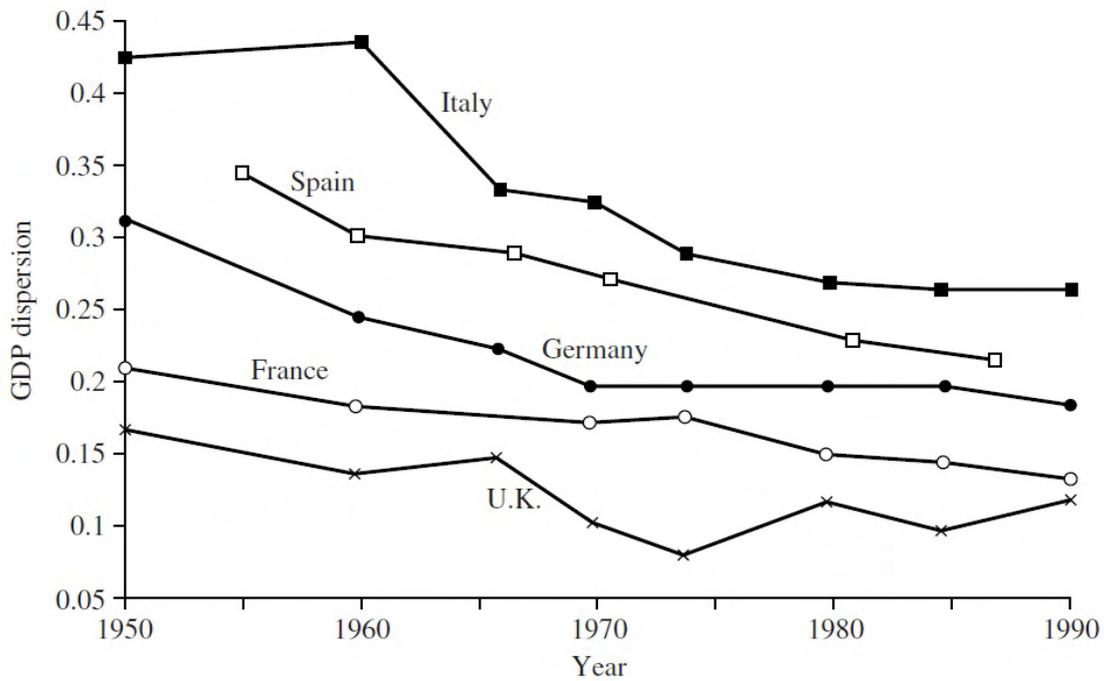
**Table 11.3**  
Convergence Across European Regions

Period	(1) Equations with Country Dummies		(2) Equations with Sectoral Shares and Country Dummies	
	$\hat{\beta}$	$R^2[\hat{\sigma}]$	$\hat{\beta}$	$R^2[\hat{\sigma}]$
1950–60	0.018 (0.006)	0.83 [0.0099]	0.034 (0.009)	0.84 [0.0094]
1960–70	0.023 (0.009)	0.97 [0.0065]	0.020 (0.006)	0.97 [0.0064]
1970–80	0.020 (0.009)	0.99 [0.0079]	0.022 (0.007)	0.99 [0.0077]
1980–90	0.010 (0.004)	0.97 [0.0066]	0.007 (0.005)	0.97 [0.0064]
Joint, 4 subperiods	0.019 (0.002)	— —	0.018 (0.003)	— —
Likelihood-ratio statistic ( <i>p</i> value)	4.9 (0.179)		8.6 (0.034)	

**Two concepts of convergence: EU8**  
 Convergence relative to the country mean



**Two concepts of convergence: EU8**



**Two concepts of convergence: EU8**

	$\beta$	$\sigma$	interesting
Germany	2,4%	0,31-0,19	
UK	2,8%	0,17-0,12	*
Italy	1,5%	0,42-0,27	*
France	1,2%	0,21-0,14	
Spain	1,8%	0,35-0,22	

*How could we explain the differences? - homework!*

**A different model: Quah**

Danny Quah: Convergence Clubs

- What if there appear plenty of connections within a group of countries, wherefore individual growth cannot explain precisely the convergence path?
- Empirical results: instead of unconditional convergence, evolving two groups and countries converge to one of these two 'peaks'
- =  $\sigma$ -convergence within the two groups
- = 'twin peaks'
- e.g. Asian convergence and EU convergence to a different level

**A different model: Quah**

